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Article

Development of a Size-Based Multiple Erosion Technique to Estimate the Aggregate Gradation in an Asphalt Mixture

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Abstract. Image processing (IP) techniques have recently been applied in the field of asphalt materials to help identify aggregate particles and measure their geometrical information based on sectional images of the material. This study examined IP techniques to improve the accuracy of analyzing the size distribution of aggregates in an asphalt mixture, and proposed two new methods: seven-layer overlaying (SLO) and size-based multiple erosion (SBME) to solve the problem of identifying connected aggregate particles that often occurs in typical IP applications. The proposed methods were tested for their effectiveness with a typical IP method using a referenced sectional image of asphalt mixture. Both the proposed methods successfully improved the accuracy of detection (number and size distribution) of aggregate particles, but the SBME approach was superior over the SLO method.

Keywords: Image processing, aggregate gradation, watershed, image morphology.

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1. Introduction

The geometrical shapes and size distribution of aggregates are key factors in the performance of asphalt mixtures for building materials [1]. A conventional method of determining these properties involves extracting the bituminous binder out of the asphalt mixture and then running sieve measurements of the remaining aggregate particles [2]. These processes are both time and man-power consuming. Recently, image processing (IP) techniques have been applied to estimate the geometrical properties of aggregates in asphalt mixtures and Portland cement concrete by applying computer software processes to images of sectional cuts to calculate the sizes, areas, perimeters and gradation of aggregate particles when the materials [3-15]. Some of key articles are summarized as follows.

Bruno et al. [3] used asphalt mixture section images to find two thresholds, black and white, to separate the images into the said colors using the Otsu method. Then they used Canny Edge Detection to find the edges of each particle and separated the connected particles using Watershed Segmentation by comparing the average estimated aggregate gradation, calculated from the single aggregate section images determined for each asphalt section, and that of the mixture. Very small differences in values were found between the two.

Vadood et al. [4] used 15 asphalt mixture section images to compare two binary methods (shape and color space methods). The image results obtained from the color space method were better than those from the shape method. The slices were scanned via an Hp-Scanner 2420 with 600 dpi resolution. The shape method used the shape of the intensity histogram to classify bituminous mastic and aggregate. For the colour space method, the bitumen and aggregate were converted into dark green and purple red, which could more accurately and easily remove bitumen from the cross-sections images than the shape method. The colour space method was selected for threshold segmentation and watershed transform (WT) was applied on the obtained binary images. Each grain in binary was determined for its area, major and minor axes of the ellipse, and these were then used to estimate the aggregate gradation. From fitting the equation and the colour space system, the obtained results indicated that the method could detect aggregate gradation with a high accuracy and could be used as a satisfactory alternative to other expensive methods.

Barbosa at al. [5] used concrete section images to find thresholds and make binary images. Then they calculated the gradation by IP and used the diameter to separate the size distribution, and then compared the results between the image and manual results. The gradation of the two techniques was found to be similar and so their proposed technique offered a low cost and effective means of evaluating the gradation of aggregates in concrete samples. The concrete sections to be analysed could be obtained via conventional parroting or sawing procedures, while the images could be taken with the help of an ordinary digital photo camera, and so there was no need for sophisticated or expensive equipment to achieve good results.

Kwan et al. [6] used three types of the aggregate images (granite, volcanic and gravel) of 10–20 mm in size to calculate the elongation index by IP in comparison with the manual technique. The obtained image results could replace the manual results. Then the digital IP (DIP) measurement results were compared to the elongation indexes obtained by the traditional method, where those obtained by the DIP method were found to be very similar to those obtained by the traditional method, but the mean elongation ratio was proposed to be a better measure of elongation than the elongation index. The DIP method was much faster to conduct and so may be a better alternative for particle shape measurement. In fact, the DIP method yielded more information about the particle shape than the manual method. With the DIP method, it was possible to measure the mean thickness/breadth and length/breadth ratios of the aggregate directly, rather than just the proportion of flaky or elongated particles according to arbitrary definitions.

You et al. [7] used X-ray computed tomography (CT) imaging to make two-dimensional (2D) horizontal slices, and then simulated a three-dimensional (3D) model of the asphalt mixture samples and made 2D vertical slices from the 3D model. In the 2D model, they calculated the areas of air void, sand mastic and aggregate to calculate the stress and strain and then predicted the dynamic modulus using the fraction of stress and strain, while in the 3D model the volumes of the same things were calculated and then compared to the 2D model. If the densities of the mastic and aggregates were not close, the images of the asphalt mixture samples were clearer and colour segmentation was easy to separate. They compared both 2D and 3D distinct element models to simulate and predicted the dynamic modulus of asphalt mixtures from its constituent properties (i.e., aggregate and mastic properties). Comparison of the modulus predictions from the 2D and 3D models revealed that the 3D models yielded a higher modulus than the 2D models.

Bessa et al. [8] characterized the three different types of aggregates (construction and demolition waste (CDW), granitic and steel slag) and the internal structure of hot mixed asphalts (HMAs) composed of those aggregate types with different gradations. They also examined the aggregate shapes in terms of the percentages of flat/elongated particles, angularity and roundness. The results obtained from different software showed that the use of DIP led to more complete and accurate results.

Chawla et al. [9] used image processing to make a 3D model of aggregate samples. They compared the 3D microstructure of particle-reinforced metal matrix composites with the three structures of (i) irregular shapes, (ii) multi-particle spheres and (iii) multi-particle ellipsoids. Then they used the 3D model to calculate the Young's modulus of each sample in comparison to that obtained from the manual method, where no significant differences were noted. Moreover, comparison of the single- and multi-particle models of simple shapes (spherical and ellipsoidal) revealed that the 3D microstructure-based approach was more accurate in simulating and understanding macroscopic and microscopic material behaviours.

Guo et al. [10] compared three methods to find gradation. In the first method, they used 2D images of aggregate samples, using the areas to replace the mass of each aggregate. In the second method, they used a 3D model, based on the stereological technique, to calculate the gradation using the sphere volume to replace the mass of the aggregate. In the final method, their 3D model used an ellipsoid to replace each aggregate. The 3D ellipsoid method yielded the best result, where the estimated errors were lower than those of the other methods. The aggregates could be assumed to be ellipsoidal particles in stereological conversion. They found that the combined method of DIP and stereological conversion was a universal, fast and accurate method for gradation estimation.

2. A Typical Method for Determining the Aggregate Geometry from an Image

2.1. Identifying Aggregate Particles

Typically, a scanned image of an asphalt mixture section reveals a blend of aggregate particles and asphalt binder. Their base colors are the basic distinction to separate aggregate particles from asphalt binder, where the asphalt binder is black and the image of each aggregate particle is comprised of inner grey pixels representing an aggregate body of limestone.

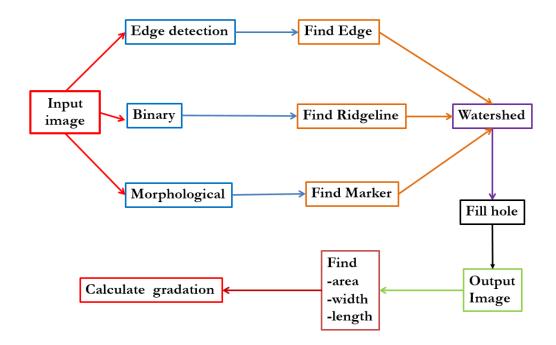


Fig. 1. Methods for the image processing to analyze the aggregate image.

According to Fig. 1, a typical image processing method [11-20] starts from using an input greyscale TIF image file, one at a time, and analyzes them by edge detection, morphological segmentation and binary

imaging. The edge detection is used to find the edges of the aggregate particles from their basic appearance, as shown in Fig. 2. The binary method is used to find ridge lines which separate aggregate territories, while the morphological segmentation is used to find markers of the approximate positions of aggregate particles. Afterwards, the image results from the three methods are received and are used later in the WT process to finally separate aggregate particles from the image background (Fig. 2e). The WT method is effective in the separation of connected aggregates and is widely used by many researchers [21-24]. The WT finds "catchment basins" and "watershed ridge lines" in the image by treating them as a surface where light pixels were high and dark pixels are low.

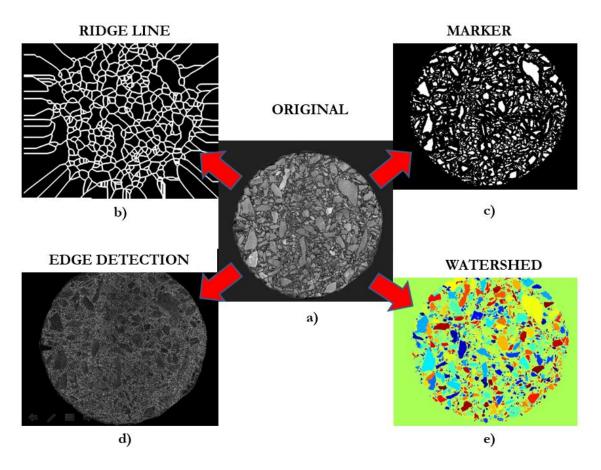


Fig. 2. (a) Image input, (b) ridge line, (c) marker, (d) image after edge detection and (e) WT segmentation.

In the WT process, the approximate shape of the aggregates was selected from diamond, circle, line and octagon (Fig. 3), where the diamond shape was found to be the most suitable, because the shape is closest to that of actual aggregates.

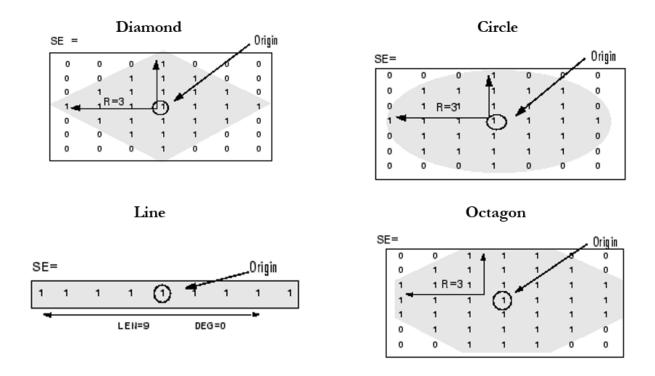


Fig. 3. Examples of shape structures used to fit the aggregate [25].

In the binary image output from the WT method, there was typically some noise found in the aggregate bodies (Fig. 4), which produced errors in identifying aggregate particles. Accordingly, the hole-filling technique [26, 27] was applied to eliminate these noises (Fig. 4). Afterwards, a particle image analysis was used to use the pixels in the particle to calculate the area, width, length and perimeter of each particle and to count the number of particles.



Fig. 4. Examples of the hole-filling technique. (a) Image with noise before and (b) after (the output) the hole-filling technique.

2.2. Determining the Dimensional Properties of Aggregates

To find the dimensional properties, such as area, width and length, of the aggregates, the ImageJ software [28] was used to create images of individual aggregate particles prior to counting them and determining their dimensions (Fig. 5).

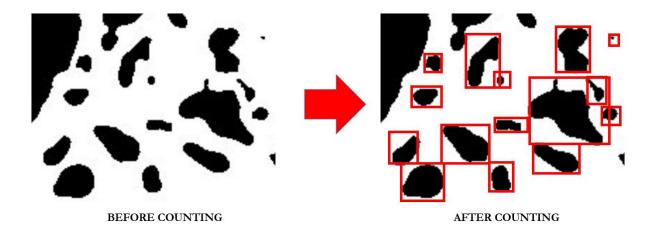


Fig. 5. Counting of aggregates.

Here Feret's diameter [29] was applied to determine the dimension of each aggregate particle, where the length is the maximum distance from one end to the other end of an aggregate particle and the width is the maximum distance that is perpendicular with the length from one end to the other end of the aggregate particle. The width of each aggregate particle was used to classify its sieve size (Fig. 6). If the width of the aggregate was smaller than the sieve size, it could pass that sieve. The area of an aggregate particle is calculated by counting the number of pixels (Fig. 7) and multiplying by the pixel unit size (mm/pixel).

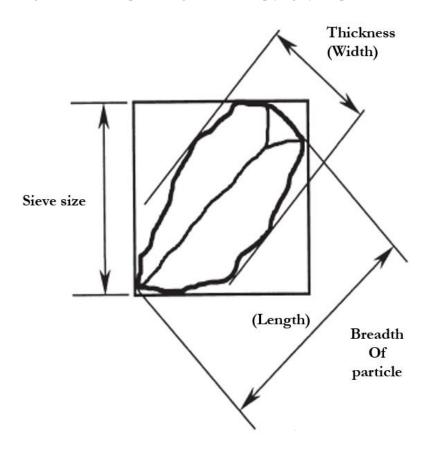


Fig. 6. Length, width and sieve size of an aggregate [30].

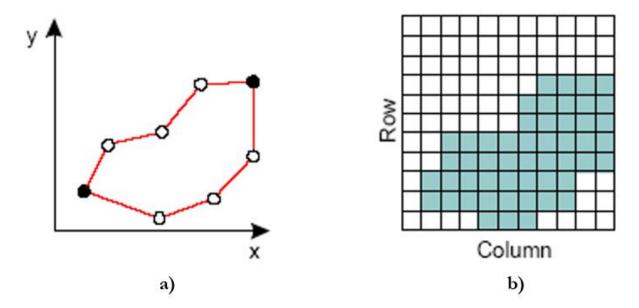
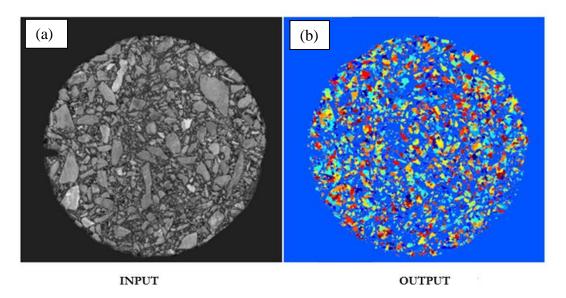


Fig. 7. Measurement of area. The (a) actual area and (b) pixel area from computer [31].

3. Problems Statement and Proposed Alternatives

However, some problems were commonly found in analyzing the process that can possibly lead to errors in the aggregate geometry. Firstly, we found over-segmentation, where aggregates are separated excessively into smaller particles than their actual sizes (Fig. 8b). This was caused by using too small a pixel value to fit various shapes of the aggregates. Secondly, we found under-segmentation, where aggregates were separated into larger particles than their actual sizes due to using too large a pixel value to fit the shapes of the aggregates (Fig. 8c).



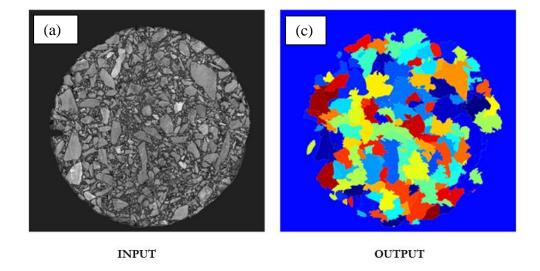


Fig. 8. The (a) input image of the cross-section and the resulting (b) over segmentation and (c) under segmentation

Lastly, we found the connected aggregate problem, in which some connected aggregate particles were identified as a single particle (Fig. 9). This problem affected the accurate counting of the number of particles.

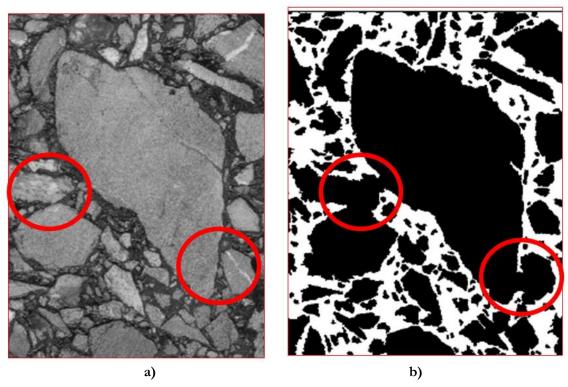


Fig. 9. Connected aggregate problem after WT segmentation. (a) Eight-bit greyscale image and (b) binary image with WT segmentation

In this paper, two new methods to separate particles from their contact appearance are introduced. These are the seven-layer overlaying (SLO) and size-based multiple erosion (SBME) methods. In order to evaluate their effectiveness in reducing errors, the results obtained from using the two methods were compared with that obtained from manually separating the particles using photo editing software.

3.1. Method A: SLO

The SLO method begins with the two outputs of colored images produced from the WT method. The two colored images (Figs. 10a and b), which are different in their number of pixels specified in the WT method, were converted to binary (black and white) images and then the hole-filling technique was applied to the two binary images (Figs. 10c and d). Next, the white area of the hole-filled images was used to check the consistency of the two images. If the pixels in the two hole-filled images are both white at the same spot, the pixel color of the larger pixel image was assigned to the pixel on the smaller pixel image. The output image (Fig. 10e) was overlaid for layers number one and two. In the next step, the output image from the previous step was taken as the smaller pixel image to be compared with the next larger pixel colored image (layer 3). These steps were repeated until the colored images of seven different pixel sizes were processed, giving seven layers.

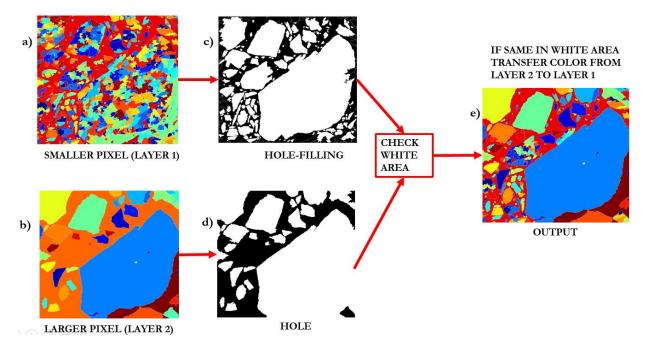


Fig. 10. The SLO method.

The advantage of the SLO technique is that it is possible to merge broken fragments in the aggregate images for better accuracy in calculation. However, some broken fragments are unnecessarily merged, leading to errors in calculating the areas of aggregate images. In Fig. 11, it starts from a greyscale input image (#0) and then images (#1) to (#7) present the seven colored images produced from using 6, 9, 15, 18, 24, 27 and 30 pixels, respectively, for the diamond shape in the WT method, leading to the output SLO image (#8).

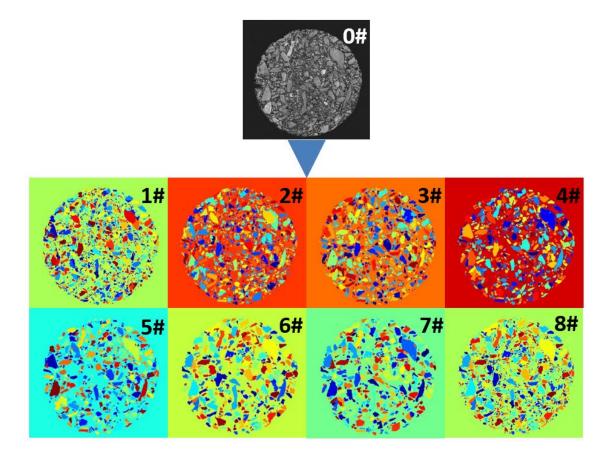


Fig. 11. Input image (#0), and each subsequent image layer processed by WT with a different number of pixels to result in seven layers (1–7#) and then form the final image (8#) after overlaying the seven layers.

3.2 Method B: SBME

In the SBME method, the erosion technique was used to solve the connected aggregate problem. After erosion, it was possible to separate the images of connected aggregates, as shown in Fig. 12. However, the problem of the erosion technique is that if the erosion is conducted with too large a pixel-value, images of small fragments of aggregates would then be completely eroded and disappear (Fig. 12b).

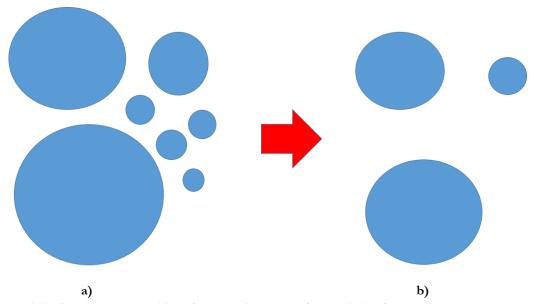


Fig. 12. Particle disappearance problem from erosion. (a) Before and (b) after erosion.

Given that different aggregate sizes would require different pixel-values to erode, then the input image was separated according to the aggregate sizes before the erosion. The separated images were then eroded with different pixel-values suitable for each aggregate size (see below).

This process started with the input image from an image scanner (Fig. 13a) and then underwent the WT technique using a diamond shape of 6-pixel size (Fig. 13b). The edges of fragments, which appear as a white colored pixel in the colored image, were detected and copied in a black colored binary image (Fig. 13c). The binary image with fragment edges was copied and then processed with the hole-filling technique (Fig. 13d), prior to separating into four images according to the four aggregate sizes (Fig. 13e) using pixel values of 1–10,000, 10,001–30,000, 30,001–50,000 and \geq 50,001 (Fig. 14). Each separated image was then eroded with the preselected suitable pixel number for each aggregate size (Fig. 13f) of 4, 20, 30 and 60 pixels for the aggregates with 10,001–30,000, 30,001–50,000 and \geq 50,001 pixels, respectively.

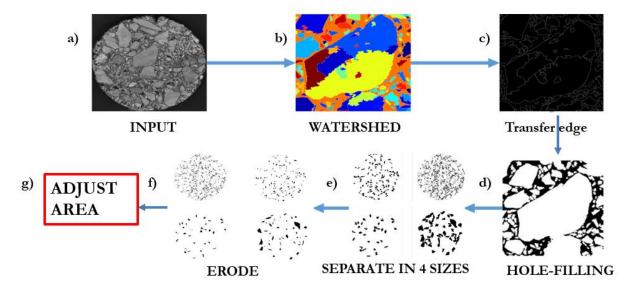


Fig. 13. Process of the SBME method.

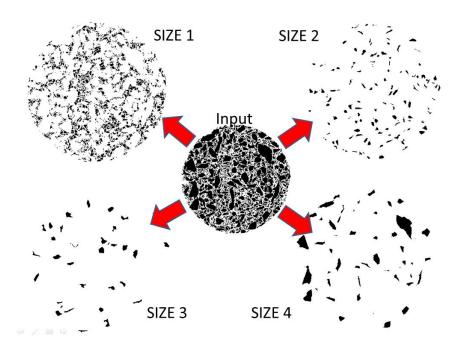


Fig. 14. Separation into the four aggregate particle sizes of particle size 1 (1–10000 pixels), particle size 2 (10001–30000 pixels), particle size 3 (3000–50000 pixels) and particle size 4 (\geq 50001 pixels).

The images after the erosion technique were then used to calculate the area, width, length and perimeter of each aggregate. Although erosion was effective in separating connected aggregate images, it reduced some aggregate areas, leading to an inaccurate calculation. Thus, the aggregate perimeter and area need some adjustment. Since the aggregate particle was reduced by the thickness of the number of eroded pixels times the unit pixel size (mm/pixel), its perimeter was first lengthened. The adjusted aggregate perimeter was calculated using Eqs. (2)–(4), based on the assumption in Fig. 15, where the adjusted area was calculated using Eq. (5).

$$Pe = 2 \pi Re, \tag{2}$$

$$Ra = Re + H, (3)$$

$$Pa = 2 \pi Ra, \tag{4}$$

$$Aa = Ae + Pa \cdot H, \tag{5}$$

where Pe is the perimeter of the eroded aggregate particle, Re is the equivalent radius of the eroded aggregate particle, H is the thickness of erosion, and is equal to the number of eroded pixels x unit pixel size (mm/pixel), Ra is the equivalent radius of the adjusted aggregate particle and Pa is the perimeter of the adjusted aggregate particle.

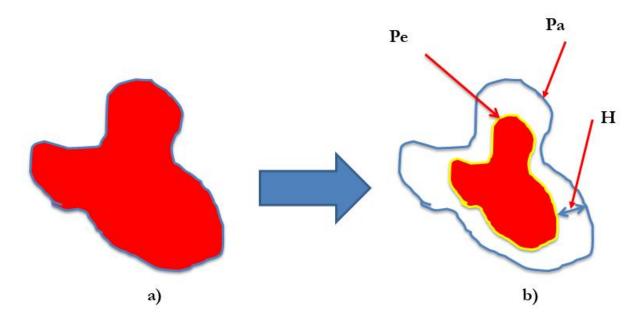


Fig. 15. Perimeter adjustment showing the particle (a) before and (b) after erosion.

4. Verification of the Proposed Methods

In order to verify the accuracy (validity) of the proposed SLO and SBME methods, the sectional image of the prepared asphalt mixture sample (Fig. 16) was used in the image processing analysis. The sample was obtained from a previous known mix design and was classified as a dense graded mixture of 12.5 mm nominal maximum aggregate size [32].

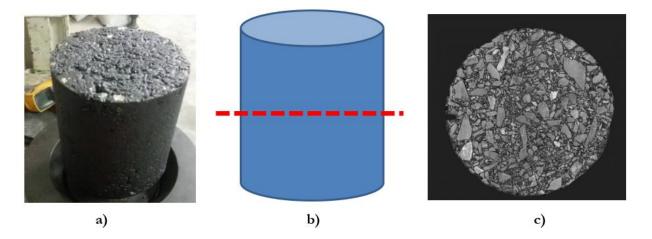


Fig. 16. Creation of sectional image of an asphalt mixture cylinder. The (a) asphalt concrete sample, (b) horizontal saw cut and (c) sectional image.

The asphalt mixture section was scanned to an 8-bit greyscale TIF file and all the connected aggregate particles in the image were separated manually using a photo editing software (Fig. 17). This image was then used as the reference in comparison with the results obtained from the SLO and SBME methods. The reference image was processed through the typical method for determining aggregates described earlier to obtain the referenced dimensions, areas and perimeters of aggregates for comparison.

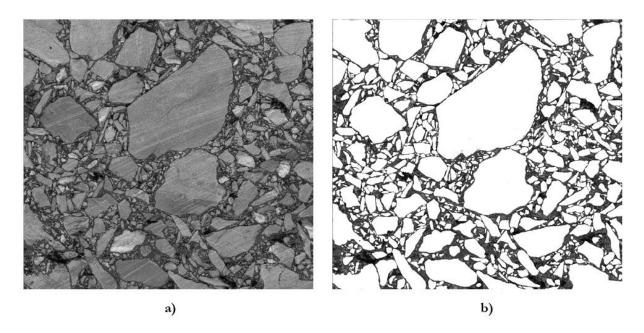


Fig. 17. (a) Scanned image input and (b) after separating connected aggregates manually using photo editing software.

The proposed SLO and SBME methods and the ordinary WT method were then applied to the raw scanned image file to obtain the dimensions, areas and perimeters, and then the results from the four methods were compared statistically. The verification process is outlined in Fig. 18.

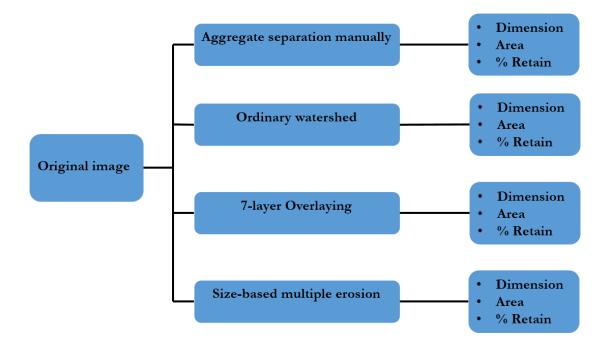


Fig. 18. Verification of the proposed methods.

The percent retained on sieve sizes [33] was the key index used to validate the effectiveness of the proposed methods. In the analysis, each aggregate particle volume could not be calculated since only a sectional area of the aggregate particle was available. Thus, a modified percent retained on sieve size by area was calculated using Eq. (6) to resemble the percent retained by weight definition [33];

% Retained by area =
$$\frac{\sum_{i=1}^{n} a_i}{A_{total}} \times 100,$$
 (6)

where a_i is the aggregate image area of the particle, $\sum_{i=1}^{n} a_i$ is the summation of aggregate image areas of all particles retained in that sieve size and A_{total} is the sectional area of the asphalt mixture.

5. Results and Analysis

The percent retained by area obtained from the four methods are shown in Table 1 and Fig. 19, while Table 2 summarizes the number of aggregate particles counted in the sectional image. The results revealed that the regular WT method produced significant errors in the number of aggregate particles detected and the percent retained on sieves compared to the manual separation method. The sum square errors in Table 2 revealed that the proposed SLO and SBME methods had fewer errors than the regular WT method. The SBME method yielded the most similar results to the referenced manual separation method, while the SLO method did not match the accuracy of the size-based multiple erosion method.

328

Table 1.	Percent	retained l	by area	for	each	method.
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Aggregate sieve size (mm)	%Retained by area			Error ²			
	Manual	SLO	SBME	WΤ	SLO	SBME	WΤ
12.7	0	2.7	0	0	7.29	0	0
9.5	1.9	5.1	2.1	3.2	10.24	0.04	1.69
4.75 (#4)	13.7	16.9	17.1	17.5	10.24	11.56	14.44
2.38 (#8)	18.6	13.4	20.6	26.3	27.04	4.00	59.29
< 2.38	20.5	14.4	18.3	13.7	37.21	4.84	46.24
Sum					92.02	20.44	121.66

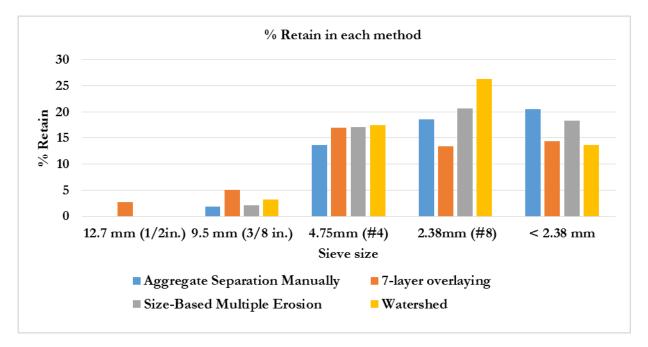


Fig. 19. Comparison of the percent retained of four methods: manual separation by photo editing software, SLO, SBME and ordinary WT.

Table 2 Number of aggregate particles counted in the sectional image.

Sieve size	Amount of aggregate				Error ²		
(mm)	Manual	SLO	SBME	WT	SLO	SBME	WT
12.7	0	1	0	0	1	0	0
9.5	1	4	1	3	9	0	4
4.75 (#4)	29	38	25	32	81	16	9
2.38 (#8)	113	91	113	102	484	0	121
< 2.38	832	580	824	750	63504	64	6724
Total	975	714	963	887	64079	80	6858

6. Conclusion

In this study, two new IP methods (SLO and SBME) for identifying aggregate particles in a sectional image of asphalt mixture were proposed to solve the problems of over or under segmentation and connected particles. The proposed methods were verified with a referenced asphalt mixture sectional image, where

they were found to be able to identify the aggregate particles more accurately than a normal WT method. The SBME method yielded the best results in identifying the number of aggregate particles and calculating the percent retained on each sieve size.

Although, the SBME method was able to provide more accurate identification of aggregate particles contained in a sectional image sample of HMA. However, applying the method as an acceptable alternative to the conventional sieving method still need further works to account on the key issues such as the real three-dimensional appearance of aggregate particles and the statistical evaluation of the new alternative method in comparison to the conventional sieving method. In the next stage, the authors plan to extend the verification of the new method by producing a number of sectional image analysis and laboratory sieved samples for statistical evaluation of the new and the conventional methods.

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